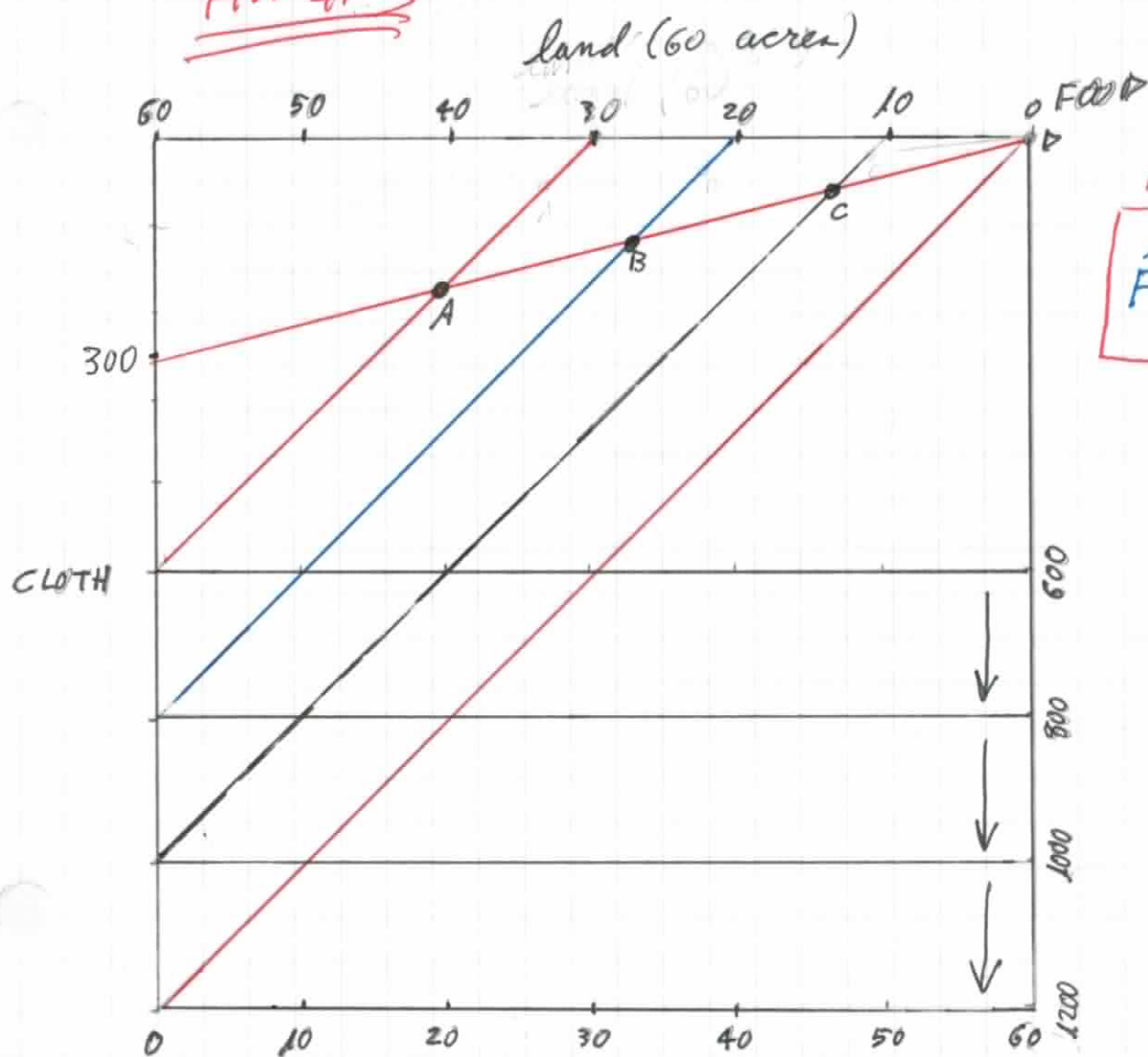


HW #3



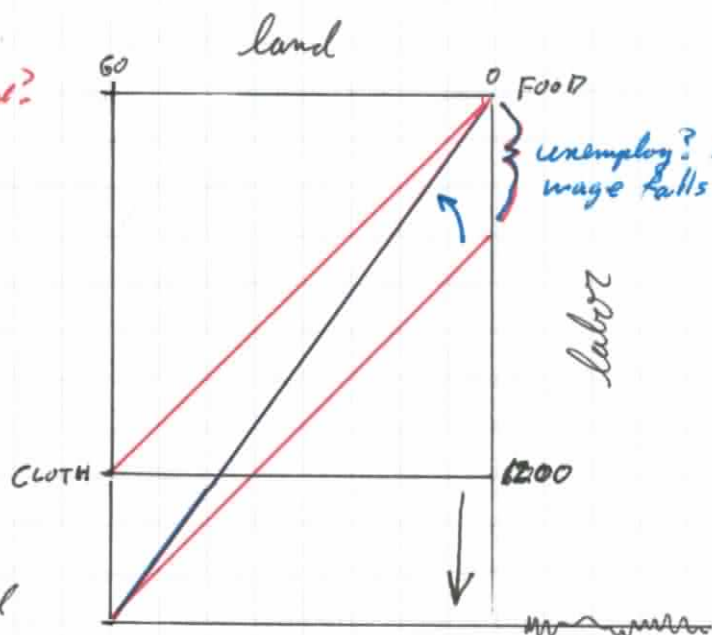
→ to draw this note that if all land employed in food sector then (at 5 hrs labor per acre of land) 300 hrs of labor would be employed on 60 acres of land & if all labor employed in cloth sector, then (at 20 hrs labor per acre of land)

hrs labor	600	800	1000	1200
acres land	30	40	50	60

→ as labor expands, more & more LAND + LABOR employed in the cloth sector until no food produced at all

→ what if we were to expand labor even further? would some labor become unemployed?

NO. wage rate would fall which would encourage cloth sector to use a higher labor to land ratio in production  
still no food produced



X

4. US labor movement's advocacy of ~~import~~ restrictions on imports from less affluent (i.e. labor abundant, low-wage) countries

- poor policy for capital abundant US
- rational policy from standpoint of US blue-collar workers, who work in labor-intensive, import-competing sectors

Note: Answer assumes HO model

Ricardian → everyone gains

Specific Factors → workers could exit "cloth sector" + enter "computer sector" (w/ trade ~~has~~ has ~~only~~ ambiguous effect on labor in Specific Factors Model)

5.

$$\frac{W_{SE}}{W_{FW}} = 0,8 \text{ failure of Factor Price}$$

Equalization due to

differences in technology between SE + FW

why? US is ~~an~~ like one big free-trade zone  
so goods prices must be equal

one would also assume that both  
SE + FW produce similar set of goods  
(agri, manuf + services)

only remaining assumption in technology

US-Mex wage differential may be due to  
combination of factors:

- techno differences
- NAFTA may not have completely equalized  
goods prices (i.e. farm subsidies)

I'd be hesitant to say that US or Mex doesn't  
produce one of the goods in question

~~But~~ Maybe there are a few specific items that  
Mex produces + US doesn't but ~~with~~  
primary set of industries should be similar

Ex. Maybe US doesn't produce tacos  
but does US produce food? **YES**

6. Leontief Paradox - see notes from lecture

7. international differences in the efficiency of factors of production make the model a bit more "Ricardian"

- Ricardian model  $\rightarrow$  Bill & Colleen were compensated acc to their productivity
- countries w/ higher productivity (i.e. more efficient factors of prod) have higher wages

*X*

### Questions for Grad Students

#### Magnification Effects

1. in the absence of joint production each price change is a positive weighted average of all factor price changes

$$\text{ex. } a_{LM} W + a_{TM} r = p_M$$

but when there's joint production <sup>RICARDIAN-STYLE</sup> each factor price change is a positive weighted average of all output price changes

$$\text{ex. } a_{LM} W + \cancel{a_{TM} r} = b_{AM} p_{AM} + b_{BM} p_{BM}$$

$\uparrow$  zero in Ricardian Model

which would reverse the Stolper-Samuelson result

## 2. "natural friend" + "natural enemy"

### "natural enemy"

- Stolper - Samuelson  $\rightarrow$  for a change in the price of each good there will exist some factor that loses in real terms
- Rybczynski  $\rightarrow$  for an increase in the endowment of each factor, there must be a good whose output falls

### "natural friend"

- Stolper - Samuelson  $\rightarrow \frac{w_i}{p_j} > 1$

An increase in  $p_j$  increases  $w_i$

if  $w_i > p_j$  then good  $j$  is natural friend of factor  $i$  i.e. increase in  $p_j$  raises real return to factor  $j$

- Rybczynski  $\rightarrow$

3. In even case each factor has a natural enemy, but does not ~~not~~ necessarily have a natural friend

4. Uneven case  $\rightarrow$  Specific Factors

$$\hat{r}_T < \hat{p}_F < \hat{w} < \hat{p}_M < \hat{r}_K$$

labor has neither natural enemy  
nor natural friend

*Handwritten flourish*

5. Empirical Tests of HO Model

a. Leontief had input-output accts  
for US econ, which enabled him  
to compute amts of capital + labor  
in each industry for 1947

He also had trade data for 1947

	Exports	Imports
Capital	\$2.5 mln	\$3.1 mln
Labor	182 person yrs	170 person yrs
K/L	\$13,700 per person yr	\$18,200 per person yr

$<$

→ His calculations measured both *direct* + *indirect* use of K+L

- *direct use* - by exporting/importing industry
- *indirect use* - by intermediate goods producing industry

→ If assume US was Kapital abundant in 1947, US should have had higher K/L ratio in exports

### HOV Model

$$\begin{pmatrix} a_{1L} & a_{1K} \\ a_{2L} & a_{2K} \end{pmatrix} \begin{pmatrix} Y_1^i - D_1^i \\ Y_2^i - D_2^i \end{pmatrix} \equiv \begin{pmatrix} F_L^i \\ F_K^i \end{pmatrix}$$

FACTOR CONTENT OF TRADE

technology matrix

↑  
vector of ~~output~~  
industry output

←  
vector of industry demand

*demand for factors:*

$$\begin{pmatrix} a_{1L} & a_{1K} \\ a_{2L} & a_{2K} \end{pmatrix} \begin{pmatrix} Y_1^i \\ Y_2^i \end{pmatrix} = \begin{pmatrix} L^i \\ K^i \end{pmatrix} \equiv V^i \quad \text{endowments}$$

### 3 ASSUMPTIONS

1. trade equalizes product prices
2. countries have identical & homothetic preferences  $\pi_x = \pi_y = 1$
3. if trade balanced

then:  $AD^i = \underbrace{A^i AD^w}_{\text{balanced trade}} = A^i AY^w = A^i V^w$

HOV then

$$\underbrace{A(Y^i - D^i)}_{\text{defined as } F^i} = V^i - A^i V^w$$

$$\begin{pmatrix} a_{KL} & a_{2L} \\ a_{LK} & a_{2K} \end{pmatrix} \begin{pmatrix} Y_1^i - D_1^i \\ Y_2^i - D_2^i \end{pmatrix} = \begin{pmatrix} K^i \\ L^i \end{pmatrix} - A^i \begin{pmatrix} K^w \\ L^w \end{pmatrix}$$

$$\begin{pmatrix} F_{2K}^i \\ F_{2L}^i \end{pmatrix} = \begin{pmatrix} K^i \\ L^i \end{pmatrix} - A^i \begin{pmatrix} K^w \\ L^w \end{pmatrix}$$



## Lerner's Thm

$$F_K^i = K^i - \alpha^i K^w$$

$$F_L^i = L^i - \alpha^i L^w$$

$$K^w = \frac{1}{\alpha^i} (K^i - F_K^i)$$

$$L^w =$$

$$\frac{K^i}{K^w} = \frac{\alpha^i K^i}{K^i - F_K^i}$$

$$\frac{L^i}{L^w}$$

if  $\frac{K^i}{K^w} > \frac{L^i}{L^w}$  then  $\frac{K^i}{K^i - F_K^i} > \frac{L^i}{L^i - F_L^i}$

$$\text{+ } \frac{K^i}{L^i} > \frac{K^i - F_K^i}{L^i - F_L^i}$$

if country capital abundant

relative to world  $\frac{K^i}{L^i} > \frac{K^w}{L^w}$

then capital labor ratio embodied

in prod  $K^i/L^i$  should be

greater than capital labor ratio

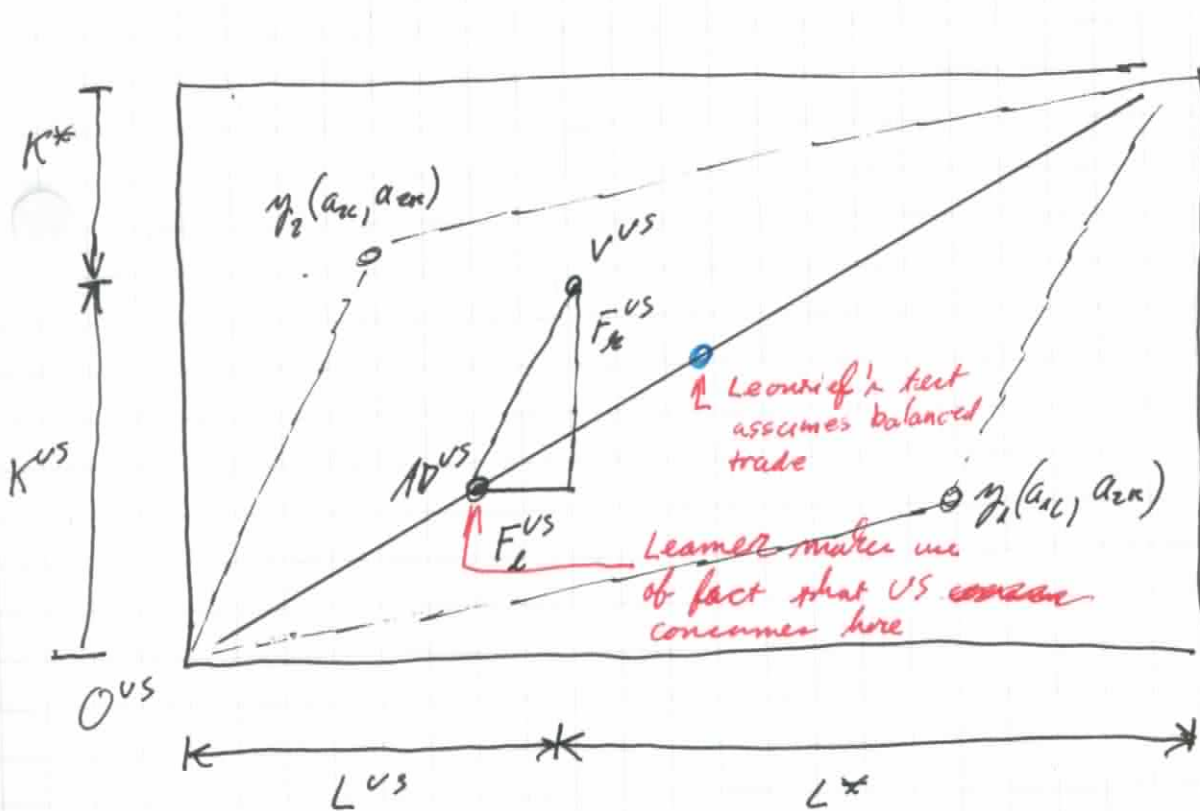
embodied in cons

$$\frac{K^i - F_K^i}{L^i - F_L^i}$$

Leamer used Leontief's data to show

	Prod	Cons
Capital	\$327 bln	\$305 bln
Labor	47 mln person yrs	45 mln person yrs
K/L	\$6950/person yrs	\$6740/person yrs

$$\frac{K^i}{L^i} > \frac{K^i - F_K^i}{L^i - F_L^i}$$



1947

$$F_K^{US} > 0$$

$$F_L^{US} > 0$$

US exported both capital & labor services

6a Treffer's incorporation of factor prod into HOV model

if factor price equalisation holds in terms of effective endowments then productivity parameters should ~~not~~ be positively correlated with factor prices

Ricardian model  $\rightarrow$  more prod country has higher income

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6b Mystery of Missing Trade

$$F_x^i = K^i - s^i K^w$$

$$F_l^i = L^i - s^i L^w$$

if these eqns hold then:

$$\text{var}(F_x^i) = \text{var}(V_x^i - s^i V_x^w)$$

$$\text{but } \frac{\text{var}(F_x^i)}{\text{var}(V_x^i - s^i V_x^w)} = \text{~~0.032~~ } 0.032$$

~~6b~~ uniform techno differences bring

6c show ratio up to 0.486

6d improved sign test: slight improvement in rank test